



Inverse Modeling of Contaminated Groundwater in Thankavur City, India

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OUTLINE

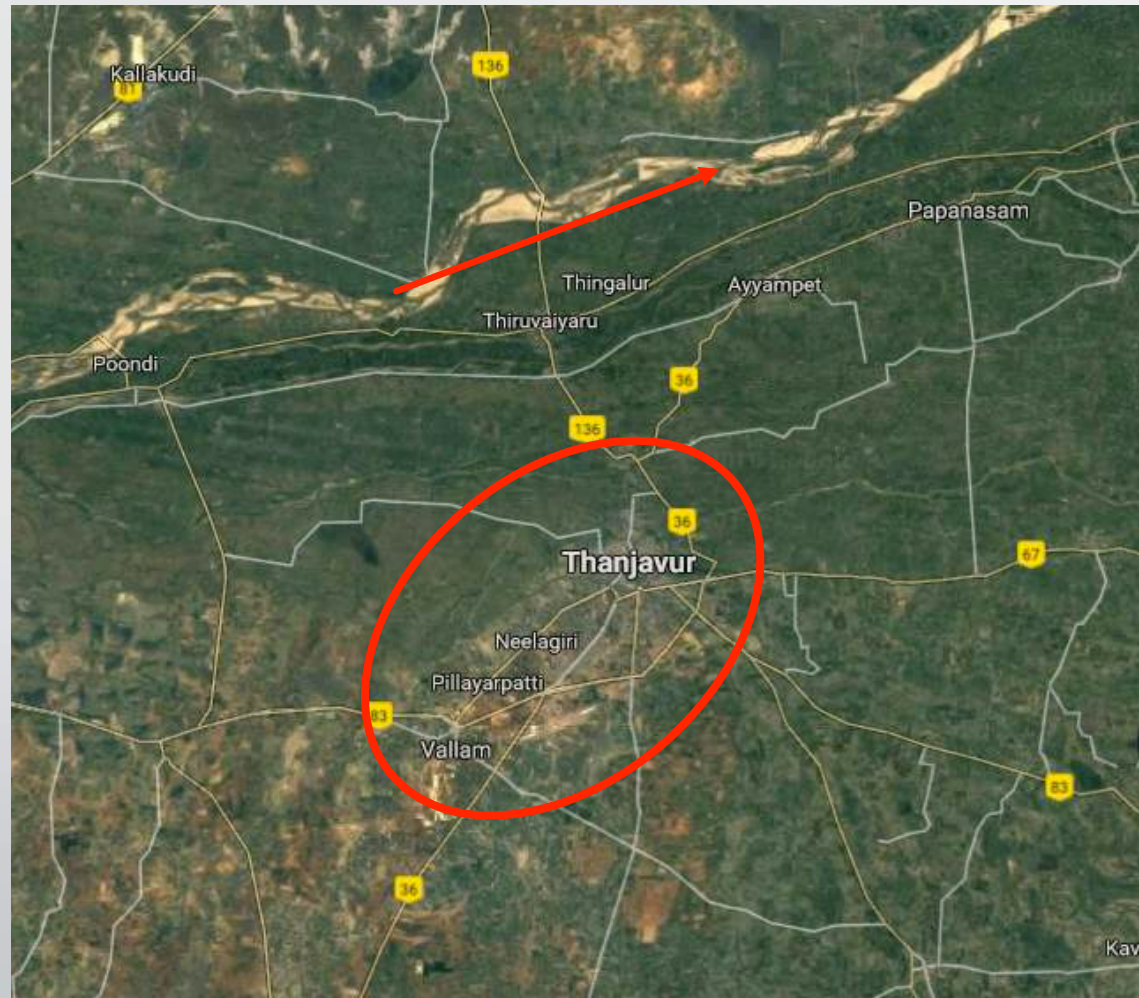
- Introduction
- Methodology
- Results and Conclusion of Initial Study
- Additional Modeling
- Conclusion of Additional Modeling

INTRODUCTION

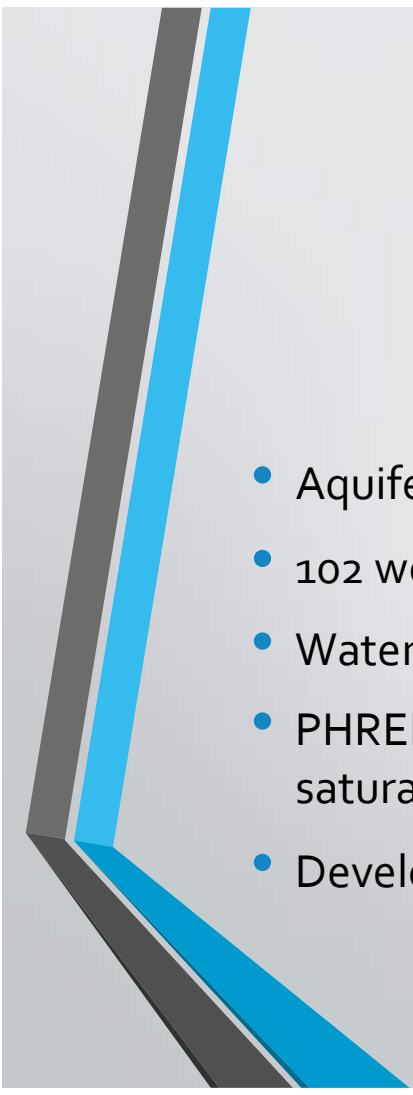
- Study area is suffering from acute shortage of good drinking water
- Groundwater is one of the main sources of water in study area
- **Objective of Initial Study:** Evaluate the groundwater quality and its suitability for domestic and agricultural activities

INTRODUCTION

- Study Area: Thanjavur City, India
- Surface Area of Aquifer: 36.31 km²
- Total Population: 226,830 (2001 Census)
- Average Annual Rainfall: 1,114 mm (Fargo, 574 mm)
- Industry: Mostly agriculture
 - 400,000 ha of agricultural land
 - Irrigated through groundwater sources and Cauvery River



Source: Google Maps



METHODOLOGY

- Aquifer divided into 10 zones
- 102 wells selected for groundwater sampling
- Water sampled in 2008
- PHREEQC used to calculate distribution of aqueous species and mineral saturation indices
- Developed groundwater quality maps

RESULTS

1. Water Sampling Analysis
2. Mineral Dissolution
3. Contamination Sources

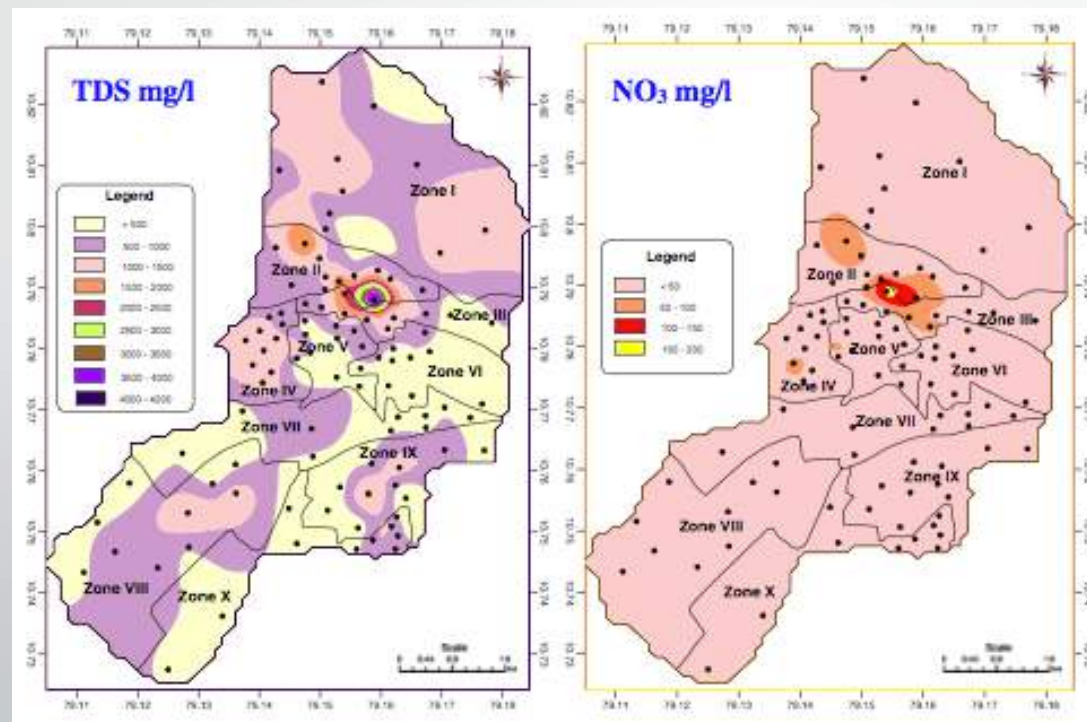
1. Water Sampling Analysis

- Initial conclusions of water sampling analysis:
 - Water chemistry in aquifer is not homogeneous
 - Chemical composition has a wide range of values
- **Research Question:** What causes the wide range of values?

1. Water Sampling Analysis

- 29.4% of samples are considered to be brackish water (TDS > 1000 mg/L)
- 96% of samples have the following distribution: Na > Ca > Mg > K
- 4% of samples have the following distribution: Ca > Na > Mg > K
- 13% of samples exceed 45 mg/L of Nitrate (EPA Standard: 10 mg/L)
- **Initial Conclusion:** A percentage of the groundwater is not safe for drinking or agricultural purposes without previous treatment.

1. Water Sampling Analysis



2. Mineral Dissolution

- SI for carbonate (calcite, dolomite), sulfate (gypsum, anhydrite), and halite minerals were calculated using PHREEQC
- **Results:**
 - SI values for sulfate and halite minerals are highly understaturated
 - No known geological formation for these minerals in study area
 - SI values Calcite and Dolomite vary throughout aquifer
 - Dissolution of carbonate minerals caused by kankar formation

3. Contamination Sources

- High concentrations of Alkalinity, Potassium, Sulfate, Chloride and Nitrate
- High TDS concentration → Saline/Brackish water present
- **Reason?**
 - Wastewater Infiltration: Leaky septic systems and sewer system
 - Fertilizer Infiltration: Washed off agricultural fields and infiltrated with rain

INVERSE MODELING

1. Inverse Modeling 101
2. Solutions Chosen
3. SI Calculation
4. Model Input
5. Choosing Appropriate Output
6. Significance of Model Output

1. Inverse Modeling 101

- Finds the sets of minerals and gasses that, when reacted in appropriate amounts, account for the differences in composition between two solutions
- Typically used for a solution traveling along a flow path
- At least 2 solutions should be used
- **Assumptions:** Homogeneous water chemistry prior to aquifer contamination
- **What are we trying to achieve?** Put a numbers to contamination sources

2. Solutions Chosen

SOLUTION 1 - Zone 9 (Average Conditions)

temp	25
→ pH	7
pe	4
redox	pe
units	ppm
density	1
→ Ca	45
Mg	16
Na	102
K	5
N(5)	9
Alkalinity	123
Cl	178
→ S(6)	19
water	1 # kg
EQUILIBRIUM_PHASES 1	
CO2 (g)	-3.5

SOLUTION 2 - Zone 2 (Maximum Conditions)

temp	25
→ pH	9.6
pe	4
redox	pe
units	ppm
density	1
→ Alkalinity	688
Ca	240
Cl	1660
K	60
Mg	154
N(5)	102
Na	740
→ S(6)	113
water	1 # kg
EQUILIBRIUM_PHASES 2	
CO2 (g)	-3.5

3. SI Calculation

SOLUTION 1 - Zone 9 (Average Conditions)

Phase	SI**	log IAP	log K(298 K, 1 atm)	
Anhydrite	-2.81	-7.09	-4.28	CaSO ₄
Aragonite	-0.79	-9.13	-8.34	CaCO ₃
Calcite	-0.65	-9.13	-8.48	CaCO ₃
CO ₂ (g)	-1.84	-3.31	-1.47	CO ₂
Dolomite	-1.40	-18.49	-17.09	CaMg(CO ₃) ₂
Gypsum	-2.51	-7.09	-4.58	CaSO ₄ ·2H ₂ O
H ₂ (g)	-22.05	-25.15	-3.10	H ₂
H ₂ O(g)	-1.50	-0.00	1.50	H ₂ O
Halite	-6.31	-4.74	1.57	NaCl
O ₂ (g)	-39.19	-42.08	-2.89	O ₂
Sylvite	-7.18	-6.28	0.90	KCl



SOLUTION 2 - Zone 2 (Maximum Conditions)

Phase	SI**	log IAP	log K(298 K, 1 atm)	
Anhydrite	-1.93	-6.21	-4.28	CaSO ₄
Aragonite	2.36	-5.97	-8.34	CaCO ₃
Calcite	2.51	-5.97	-8.48	CaCO ₃
CO ₂ (g)	-4.27	-5.74	-1.47	CO ₂
Dolomite	5.23	-11.86	-17.09	CaMg(CO ₃) ₂
Gypsum	-1.63	-6.21	-4.58	CaSO ₄ ·2H ₂ O
H ₂ (g)	-27.25	-30.35	-3.10	H ₂
H ₂ O(g)	-1.50	-0.00	1.50	H ₂ O
Halite	-4.59	-3.02	1.57	NaCl
O ₂ (g)	-28.79	-31.68	-2.89	O ₂
Sylvite	-5.24	-4.34	0.90	KCl

4. Model Input

SOLUTION 1 - Zone 9 (Average Conditions)

```
temp      25
pH         7
pe         4
redox      pe
units      ppm
density    1
Ca         45
Mg         16
Na         102
K          5
N(5)       9
Alkalinity 123
Cl         178
S(6)       19
water      1 # kg
EQUILIBRIUM_PHASES 1
CO2(g)     -3.5
```

```
INVERSE_MODELING 1
solutions        1      2
```

SOLUTION 2 - Zone 2 (Maximum Conditions)

```
temp      25
pH         9.6
pe         4
redox      pe
units      ppm
density    1
Alkalinity 688
Ca         240
Cl         1660
K          60
Mg         154
N(5)       102
Na         740
S(6)       113
water      1 # kg
EQUILIBRIUM_PHASES 2
CO2(g)     -3.5
```

- Output: 158 possible models
- Input needs to be adjusted

4. Model Input

```

INVERSE_MODELING 1
  solutions      1      2
  uncertainty    0.05   0.1
  phases
    Anhydrite    dis
    Aragonite    pre
    Calcite      pre
    CO2(g)       dis
    Dolomite     pre
    Gypsum
    H2(g)        dis
    H2O(g)       dis
    Halite
    O2(g)        dis
    Sylvite      dis
    H2S(g)
    N2(g)
    NH3(g)
    Sulfur
  balances
    K            0.05   0.05
  range          1000
  minimal
  tolerance      1e-10
  mineral_water  true
  multiple_precision true
  mp_tolerance   1e-12
  censor_mp      1e-20
  
```

- **Uncertainty:** Sets uncertainty limits for solutions
- **Phases:** List of phases to be used during inverse modeling
- **Balances:** Includes mole balance for elements not contained in the phases
- **Range:** To display min. and max. ranges in phase transfers
- **Minimal:** To reduce models to the minimum number of phases that can satisfy all constraints
- **Tolerance:** Indicates the tolerance for optimizing solver
- **Mineral Water:** Identifier to include/exclude water derived from minerals in the balance calculations
- **Multiple Precision:** Invokes multiple-precision version Cl1
- **mp_tolerance:** Indicates tolerance of multiple precision method
- **Censor_mp:** Additional identifier of the multiple precision method

5. Choosing Appropriate Output

Model #1		Model #3		Model #5		Model #7		Model #9	
Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction	
Solution 1	1.26E+01	Solution 1	1.26E+01	Solution 1	1.23E+02	Solution 1	1.23E+01	Solution 1	1.23E+01
Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00
Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers	
Anhydrite	3.23E+02	Anhydrite	3.23E+02	Anhydrite	3.14E+02	Anhydrite	3.14E+02	Anhydrite	3.14E+02
Aragonite		Aragonite		Aragonite		Aragonite	-2.42E-02	Aragonite	-2.42E-02
Calcite	-2.48E-02	Calcite	-2.48E-02	Calcite	-2.42E-02	Calcite		Calcite	
CO2(g)		CO2(g)		CO2(g)		CO2(g)		CO2(g)	
Dolomite	-1.75E-03	Dolomite	-1.75E-03	Dolomite	-1.51E-03	Dolomite	-1.51E-03	Dolomite	-1.51E-03
Gypsum	-3.23E+02	Gypsum	-3.23E+02	Gypsum	-3.14E+02	Gypsum	-3.14E+02	Gypsum	-3.14E+02
H2(g)		H2(g)		H2(g)	7.64E-02	H2(g)		H2(g)	7.64E-02
H2O(g)		H2O(g)		H2O(g)		H2O(g)		H2O(g)	
Halite	-2.06E-02	Halite	-2.06E-02	Halite	-1.91E-02	Halite	-1.91E-02	Halite	-1.91E-02
O2(g)		O2(g)		O2(g)		O2(g)		O2(g)	
Sylvite		Sylvite		Sylvite		Sylvite		Sylvite	
H2S(g)	-1.95E-02	H2S(g)		H2S(g)	-1.91E-02	H2S(g)	5.73E-02	H2S(g)	-1.91E-02
N2(g)	-2.66E-02	N2(g)	-2.01E-02	N2(g)		N2(g)		N2(g)	
NH3(g)	5.27E-02	NH3(g)	3.97E-02	NH3(g)		NH3(g)		NH3(g)	
Sulfur		Sulfur	-1.95E-02	Sulfur		Sulfur	-7.64E-02	Sulfur	
Model #2		Model #4		Model #6		Model #8		Model #10	
Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction	
Solution 1	1.23E+01	Solution 1	1.26E+01	Solution 1	1.23E+01	Solution 1	1.26E+01	Solution 1	1.23E+01
Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00
Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers	
Anhydrite	3.14E+02	Anhydrite	3.23E+02	Anhydrite	3.14E+02	Anhydrite	3.23E+02	Anhydrite	3.14E+02
Aragonite		Aragonite	-2.48E-02	Aragonite	-2.42E-02	Aragonite	-2.48E-02	Aragonite	-2.42E-02
Calcite	-2.42E-02	Calcite		Calcite		Calcite		Calcite	
CO2(g)		CO2(g)		CO2(g)		CO2(g)		CO2(g)	
Dolomite	-1.51E-03	Dolomite	-1.75E-03	Dolomite	-1.51E-03	Dolomite	-1.75E-03	Dolomite	-1.51E-03
Gypsum	-3.14E-02	Gypsum	-3.23E+02	Gypsum	-3.14E+02	Gypsum	-3.23E+02	Gypsum	-3.14E+02
H2(g)		H2(g)		H2(g)	5.73E-02	H2(g)		H2(g)	5.73E-02
H2O(g)		H2O(g)		H2O(g)		H2O(g)		H2O(g)	
Halite	-1.91E-02	Halite	-2.06E-02	Halite	-1.91E-02	Halite	-2.06E-02	Halite	-1.91E-02
O2(g)		O2(g)		O2(g)		O2(g)		O2(g)	
Sylvite		Sylvite		Sylvite		Sylvite		Sylvite	
H2S(g)	5.73E-02	H2S(g)	-1.95E-02	H2S(g)		H2S(g)		H2S(g)	
N2(g)		N2(g)	-2.66E-02	N2(g)		N2(g)	-2.01E-02	N2(g)	
NH3(g)		NH3(g)	5.27E-02	NH3(g)		NH3(g)	3.97E-02	NH3(g)	
Sulfur	-7.64E-02	Sulfur		Sulfur	-1.91E-02	Sulfur	-1.95E-02	Sulfur	-1.91E-02

5. Choosing Appropriate Output

- Criteria for selecting the right model:
 - #1: Model must have calcite, dolomite, anhydrite, gypsum and halite
 - #2: Model should have least amount of automatically added phases
 - ❖ $\text{H}_2\text{S}(\text{g})$, $\text{N}_2(\text{g})$, $\text{NH}_3(\text{g})$, and Sulfur

5. Choosing Appropriate Output

Model #1		Model #3		Model #5		Model #7		Model #9	
Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction	
Solution 1	1.26E+01	Solution 1	1.26E+01	Solution 1	1.23E+02	Solution 1	1.23E+01	Solution 1	1.23E+01
Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00
Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers	
Anhydrite	3.23E+02	Anhydrite	3.23E+02	Anhydrite	3.14E+02	Anhydrite	3.14E+02	Anhydrite	3.14E+02
Aragonite		Aragonite		Aragonite		Aragonite	-2.42E-02	Aragonite	-2.42E-02
Calcite	-2.48E-02	Calcite	-2.48E-02	Calcite	-2.42E-02	Calcite		Calcite	
CO2(g)		CO2(g)		CO2(g)		CO2(g)		CO2(g)	
Dolomite	-1.75E-03	Dolomite	-1.75E-03	Dolomite	-1.51E-03	Dolomite	-1.51E-03	Dolomite	-1.51E-03
Gypsum	-3.23E+02	Gypsum	-3.23E+02	Gypsum	-3.14E+02	Gypsum	-3.14E+02	Gypsum	-3.14E+02
H2(g)		H2(g)		H2(g)	7.64E-02	H2(g)		H2(g)	7.64E-02
H2O(g)		H2O(g)		H2O(g)		H2O(g)		H2O(g)	
Halite	-2.06E-02	Halite	-2.06E-02	Halite	-1.91E-02	Halite	-1.91E-02	Halite	-1.91E-02
O2(g)		O2(g)		O2(g)		O2(g)		O2(g)	
Sylvite		Sylvite		Sylvite		Sylvite		Sylvite	
H2S(g)	-1.95E-02	H2S(g)		H2S(g)	-1.91E-02	H2S(g)	5.73E-02	H2S(g)	-1.91E-02
N2(g)	-2.66E-02	N2(g)	-2.01E-02	N2(g)		N2(g)		N2(g)	
NH3(g)	5.27E-02	NH3(g)	3.97E-02	NH3(g)		NH3(g)		NH3(g)	
Sulfur		Sulfur	-1.95E-02	Sulfur		Sulfur	-7.64E-02	Sulfur	
Model #2		Model #4		Model #6		Model #8		Model #10	
Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction		Solution Fraction	
Solution 1	1.23E+01	Solution 1	1.26E+01	Solution 1	1.23E+01	Solution 1	1.26E+01	Solution 1	1.23E+01
Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00	Solution 2	1.00E+00
Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers		Phase Mole Transfers	
Anhydrite	3.14E+02	Anhydrite	3.23E+02	Anhydrite	3.14E+02	Anhydrite	3.23E+02	Anhydrite	3.14E+02
Aragonite		Aragonite	-2.48E-02	Aragonite	-2.42E-02	Aragonite	-2.48E-02	Aragonite	-2.42E-02
Calcite	-2.42E-02	Calcite		Calcite		Calcite		Calcite	
CO2(g)		CO2(g)		CO2(g)		CO2(g)		CO2(g)	
Dolomite	-1.51E-03	Dolomite	-1.75E-03	Dolomite	-1.51E-03	Dolomite	-1.75E-03	Dolomite	-1.51E-03
Gypsum	-3.14E+02	Gypsum	-3.23E+02	Gypsum	-3.14E+02	Gypsum	-3.23E+02	Gypsum	-3.14E+02
H2(g)		H2(g)		H2(g)	5.73E-02	H2(g)		H2(g)	5.73E-02
H2O(g)		H2O(g)		H2O(g)		H2O(g)		H2O(g)	
Halite	-1.91E-02	Halite	-2.06E-02	Halite	-1.91E-02	Halite	-2.06E-02	Halite	-1.91E-02
O2(g)		O2(g)		O2(g)		O2(g)		O2(g)	
Sylvite		Sylvite		Sylvite		Sylvite		Sylvite	
H2S(g)	5.73E-02	H2S(g)	-1.95E-02	H2S(g)		H2S(g)		H2S(g)	
N2(g)		N2(g)	-2.66E-02	N2(g)		N2(g)	-2.01E-02	N2(g)	
NH3(g)		NH3(g)	5.27E-02	NH3(g)		NH3(g)	3.97E-02	NH3(g)	
Sulfur	-7.64E-02	Sulfur		Sulfur	-1.91E-02	Sulfur	-1.95E-02	Sulfur	-1.91E-02

5. Significance of Model Output

- I. Element Mole Transfers
- II. Solution Fractions
- III. Phase Mole Transfers

I. Element Mole Transfers

Solution 1: - Zone 9 (Average Conditions)

	<u>Input</u>		<u>Delta</u>		<u>Input+Delta</u>
pH	7.000e+00	+	0.000e+00	=	7.000e+00
Alkalinity	2.459e-03	+	-1.229e-04	=	2.336e-03
C(-4)	0.000e+00	+	0.000e+00	=	0.000e+00
C(4)	2.945e-03	+	0.000e+00	=	2.945e-03
Ca	1.123e-03	+	5.617e-05	=	1.179e-03
Cl	5.023e-03	+	-3.486e-05	=	4.988e-03
H(0)	0.000e+00	+	0.000e+00	=	0.000e+00
K	1.279e-04	+	2.535e-06	=	1.305e-04
Mg	6.584e-04	+	3.292e-05	=	6.914e-04
N(-3)	0.000e+00	+	0.000e+00	=	0.000e+00
N(0)	0.000e+00	+	0.000e+00	=	0.000e+00
N(3)	0.000e+00	+	0.000e+00	=	0.000e+00
N(5)	6.429e-04	+	-3.214e-05	=	6.107e-04
Na	4.439e-03	+	0.000e+00	=	4.439e-03
O(0)	0.000e+00	+	0.000e+00	=	0.000e+00
S(-2)	0.000e+00	+	0.000e+00	=	0.000e+00
S(6)	1.979e-04	+	-9.894e-06	=	1.880e-04

Concentration
(mol/kg water) or (pH)

Input + Uncertainty

Solution 2: - Zone 2 (Maximum Conditions)

	<u>Input</u>		<u>Delta</u>		<u>Input+Delta</u>
pH	9.600e+00	+	0.000e+00	=	9.600e+00
Alkalinity	1.380e-02	+	-1.380e-03	=	1.242e-02
C(-4)	0.000e+00	+	0.000e+00	=	0.000e+00
C(4)	8.970e-03	+	0.000e+00	=	8.970e-03
Ca	6.011e-03	+	6.011e-04	=	6.612e-03
Cl	4.700e-02	+	-4.700e-03	=	4.230e-02
H(0)	0.000e+00	+	0.000e+00	=	0.000e+00
K	1.540e-03	+	6.476e-05	=	1.605e-03
Mg	6.358e-03	+	6.358e-04	=	6.994e-03
N(-3)	0.000e+00	+	0.000e+00	=	0.000e+00
N(0)	0.000e+00	+	0.000e+00	=	0.000e+00
N(3)	0.000e+00	+	0.000e+00	=	0.000e+00
N(5)	7.310e-03	+	2.033e-04	=	7.513e-03
Na	3.231e-02	+	3.231e-03	=	3.554e-02
O(0)	0.000e+00	+	0.000e+00	=	0.000e+00
S(-2)	0.000e+00	+	0.000e+00	=	0.000e+00
S(6)	1.181e-03	+	-1.181e-04	=	1.063e-03

Added Uncertainty

II. Solution Fractions

Solution fractions:			Minimum	Maximum
Solution	1	1.230e+01	1.227e+01	1.232e+01
Solution	2	1.000e+00	1.000e+00	1.000e+00

- Solution #1 (Zone 9) must be concentrated 12.3 fold to produce solution #2 (Zone 2)
- 12.3 kg of water in solution #1 is reduced to 1 kg of water in solution #2
- Look into phase mole transfers in order to find out where the 12.3 times concentration is coming from

III. Phase Mole Transfers

Phase mole transfers:		Minimum	Maximum	
Anhydrite	3.137e+02	3.129e+02	3.143e+02	CaSO ₄
Calcite	-2.424e-02	-2.701e-02	-2.146e-02	CaCO ₃
Dolomite	-1.511e-03	-1.525e-03	-1.491e-03	CaMg(CO ₃) ₂
Gypsum	-3.137e+02	-3.143e+02	-3.129e+02	CaSO ₄ ·2H ₂ O
Halite	-1.907e-02	-2.189e-02	-1.627e-02	NaCl
H ₂ S(g)	5.732e-02	4.905e-02	6.556e-02	H ₂ S
Sulfur	-7.642e-02	-8.741e-02	-6.540e-02	S

(-) Precipitation → Out of solution

(+) Dissolution → Into solution

Optimized Phase Transfers
(mol/12.3 kg water)

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(mol/kg water)

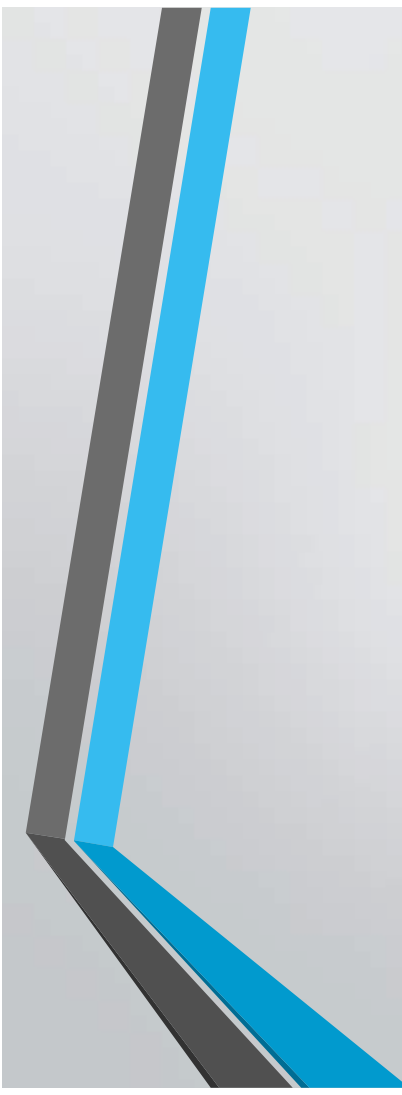
Anhydrite	2.55E+01
Calcite	-1.97E-03
Dolomite	-1.23E-04
Gypsum	-2.55E+01
Halite	-1.55E-03
H ₂ S(g)	4.66E-03
Sulfur	-6.21E-03

Conclusions

- Inverse modeling shows that within the given uncertainty limits precipitation of calcite, dolomite, gypsum, halite and sulfur, and dissolution of anhydrite can $\text{H}_2\text{S}(\text{g})$ can explain the changes in major ion composition
- Confirms that contamination is occurring

REFERENCES

- Nagaragan, R., Rajmohan, N., Mahendran, U., and Senthamilkumar, S. (2010). Evaluation of Groundwater Quality and its Suitability for Drinking and Agricultural use in Thanjavur City, Tamil Nadu, India. *Environmental Monitoring and Assessment*. 171: 289-308



Thank you!
Questions?